

Review Article

A Reappraisal of Einstein's Light-Quantum Hypothesis

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Abstract

Einstein published his light-quantum hypothesis (LH) 1905, suggesting that a light ray transmits discrete energy quanta $h \cdot f_i$, emitted at speed c from their source, where h refers to Planck's constant - and f_i to the frequency of a ray of light L_x in accordance with the wave equation $c = \lambda_i \cdot f_i$ - with λ_i indicating the wavelength of L_x . Now, let f_v and f_r stand for the frequency of violet and red light, respectively, assuming that $f_v = 2 \cdot f_r$. Following these premises, a source of light Q_v emitting $h \cdot f_v$ light-quanta would transmit an energy amounting to $(h \cdot f_v \cdot f_v)$ per second, whereas a source Q_r , releasing $h \cdot f_r$ light-quanta would only emit an energy equivalent to $(h \cdot f_r \cdot f_r)$. In other words: The LH implies that the energy a ray of light transports per time-unit corresponds to the square of its frequency. This stands at odds with the experimentally established view that the energy carried by different light-rays per time-unit is linearly proportional to their (respective) frequency.

Introduction

Einstein introduced 1905 the *light-quantum-hypothesis* (LH) in his paper «Über einen die Erzeugung und Verwandlung des Lichtes betreffenden heuristischen Gesichtspunkt» [On a heuristic point of view concerning the production and transformation of light]. With the help of the LH he aimed to interpret the photoelectric effect - as well as other phenomena related to it - in a consistent, straightforward way.

In the present paper, I shall

1. Consider the LH as a purely theoretical system, based on a number of explicit and implicit postulates;
2. Check whether the postulates underlying the LH are self-consistent and mutually compatible;
3. Analyse certain implications of the LH, and compare them with the generally accepted interpretation of the experimental findings.

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Explicit and Implicit Postulates Underlying the LH

P1: Let sources of light Q_x emit homogenous, mono-frequent rays of light L_x .

P2: Let the wave-equation

$$(1) \quad c = \lambda_i \cdot f_i$$

be valid for every light-ray L_i emitted by a source Q_i , with λ_i referring to the wavelength of a ray of light L_i , and f_i to the frequency of L_i .

P3: Let L_v be of a higher frequency than L_r , i.e. $f_v > f_r$, with 'v' standing for "violet", 'r' for red.

P4: Let every source of light Q_i which emits rays of light of a given frequency f_i , emit these rays as bundles of light-quanta or photons Φ_i having the energy $h \cdot f_i$, i.e.

$$(2) \quad E_i = h \cdot f_i,$$

where 'h' refers to Planck's constant (elementary quantum of action), and 'f_i' to the frequency.

P5: Let the light-quanta (=energy quanta, photon) Φ_i , which are emitted by Q_i , move through space as indivisible entities, and let them be absorbed as such by adequate targets.

P6: Let each light-quantum Φ_i move with speed c in relation to its source Q_i - if mutual conditions of rest are given between source, receiver, and medium (insofar a medium needs to be taken into account).

A short explanation of the foregoing postulates reads as follows:

Postulate *P1* is seldom assumed explicitly. Einstein, in his introductory remarks, observed that he would consider the energy transmitted by a light-ray emitted by a «Lichtpunkt» (i.e. a very small source of light). With respect to the following analysis, I'll assume the existence of « quasi-linear » rays of light, i.e. tiny bundles of light the cross-sections of which are so small that only one light-quantum per unit of time can hit and perforate an adequately placed perpendicular plane. Said in other terms, and in accordance with Einstein: I'll consider rays of light in which light-quanta move in a linear row.

Postulate *P2* is very rarely formulated explicitly. Nevertheless, it is implicitly taken for granted as soon as one:

- (a) alludes to the frequency f_i of a given light-ray, and distinguishes rays of light of different frequencies;
- (b) introduces c as the constant speed of every light-ray L_i in relation (i) to its source, (ii) to the medium (insofar a medium has to be considered), (iii) the receptor, and (iv) the « external

observers » - albeit on the premises that source, medium, receptor, and « external observers » are at rest with respect to each other;

- (c) assumes that the fronts of the rays of light – e.g. of violet and red light – proceed from their respective sources at equal speeds c .

Postulate $P3$ is generally accepted and needs no further comment.

Postulates $P4$ and $P5$ comprise the main, central, statements of Einstein's LH [1]. Strictly speaking, $P4$ and $P5$ contain three separate assertions, concerning:

- (i) the *emission* of light-quanta (see: $P4$);
- (ii) the *propagation* through space of indivisible light-quanta (see: $P5$), and
- (iii) the *absorption* of indivisible light-quanta (see: $P5$).

However, since I am dealing in the present paper only with the *emission* and the *propagation* of light-quanta, I have subsumed propagation and absorption to the same postulate $P5$.

Postulate $P6$ is seldom stated explicitly. In a configuration stating mutual rest of source, receiver, medium (insofar a medium needs to be considered), and observers – $P6$ is self-evident. Furthermore, $P6$ can be derived from $P2$ in conjunction with $P4$ and $P5$ [2-5].

Discussion of the LH

We shall start by considering the postulates $P1 - P6$ independently of one another: As far as I can see, there are no ambiguous demands being made, and nothing otherwise untenable can be discerned. Thus, every single postulate $P1 - P6$, taken on its own, is free from contradictions [6,7].

We must now look at several combinations of these postulates:

- (i) It follows from $P3$ and $P4$ that Lv -photons consist of a larger amount of energy than Lr -photons. In other terms:
($Ev=h.fv$) > ($Er=h.fr$).
- (ii) According to $P4$ in conjunction with $P5$, the light-quanta spread from their respective sources as indivisible entities, in their respective frequencies fv and fr – which is a constitutive factor of the light-rays we are considering.
- (iii) With regard to $P2$, it follows that every frequency fi is univocally correlated to a corresponding wavelength li , so that any kind of event belonging to Li (e.g. its wave-peaks) will be repeated with the corresponding frequency fi at any well-defined point along the path of Li that continues to move forth with speed c .
- (iv) According to $P4$, source Qv emits light-quanta of energy $h.fv$, whereas a source Qr will release light-quanta of energy $h.r$.
- (v) Now, following $P3$, ' fv ' refers to the frequency of violet light-rays and ' fr ' to the frequency of red light-rays, with $fv > fr$. On the basis of $P2$, we will then, reciprocally, have to infer that $\lambda v < \lambda r$.

This assertion implies that source Qv will not only emit light-quanta Phv which excel in energy the light-quanta Phr emitted by source Qr by the factor $(fv - fr)$, but *also* that source Qv is due to propagate its light-quanta Phv with a frequency which surpasses the frequency with which source Qr releases its light-quanta Phr by the same factor $(fv - fr)$.

In other words: On the basis of $P1 - P6$, we are compelled to deduce that if we – for instance – compare a ray of light Lv of wavelength $\lambda v=4000\text{ nm}$ with a ray of light Lr of wavelength $\lambda r=8000\text{ nm}$, the former one (i.e. Lv) must transmit *four* times (and *not* twice) as much energy per unit of time than the latter (i.e. Lr).

It is hard to see, how this unexpected implication could be avoided: The frequency fi is a firmly bound variable of equation (1) [$c=\lambda i.f i$]. – As soon as we use the symbol ' fi ' to point at the energy of a light-quantum $h.f i$, we are forced to accept that these quanta are linked to equation (1) and are, therefore, emitted fi times per unit of time.

- (vi) Einstein *believed* that the amount of energy contained in a single light-quantum $h.f i$ is *linearly proportional* to its frequency, i.e. to the fi . However, *on the basis of his premises – i.e. of his postulates $P1 - P6$ –* we are logically compelled to infer that Einstein's premises do not support what Einstein *believed to be true, but – on the contrary –* supported the erroneous assumption that the amount of energy contained in a single light-quantum $h.f i$ is proportional to the *square* its frequency.

- (vii) In 1916 [8]: Millikan pointed out: "The hypothesis [i.e. Einstein's LH] was apparently made solely because it furnished a ready explanation that when an electron is thrown out of a metal by ultra-violet light or X-rays it is independent of the intensity of the light while it depends on its frequency ." However, if one *correctly argues – based on the experimental findings established by Millikan –* that the amount of energy being transported by a ray of light Li per unit of time is *linearly proportional* to its frequency – one is compelled to dismiss as erroneous the core of Einstein's theoretical *premises and his reasonings based on them*. In short: Einstein's theoretical premises and his reasonings based on them stand at odds with his belief and with the experimental findings established by Millikan.

Conclusion

Einstein's *light quantum hypothesis* (LH) prescribes that every ray of light Li transports and transmits discrete *energy-light-quanta* of magnitude $h.f i$. If every source of light Qi emitted discrete *light-quanta* of a specific, frequency-dependent magnitude $h.f i$, it would also have to release these *energy-quanta* with the corresponding frequency fi . This would, in turn, imply that the energy Qi emitted per unit of time with a ray of light Li , had to be proportional to the square of its frequency, *i.e.* the amount of the propagated and transmitted energy would have to be equivalent to $fi.(h.f i)$ per unit of time. However, if we hold to the generally acknowledged – and by Millikan [9] experimentally established – view that every ray of light transports and transmits an amount of energy per unit of time which is linearly proportional to its frequency, Einstein's premises and his reasonings cannot be maintained.

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